

Probing New Physics in Charm Couplings with Kaon and Other Hadron Processes

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Outline of talk

- * **Introduction**
- * **Kaon processes**
- * **Other hadron processes**
- * **Conclusions**

Introduction

- * Existing data on various decays of hadrons and mixing of neutral mesons are consistent with the **loop-induced** nature of **flavor-changing neutral currents** (FCNC's) in the **standard model** (SM)
- * They are also consistent with the unitarity of the **Cabibbo-Kobayashi-Maskawa** (CKM) matrix with three generations.
- * Our understanding of the dynamics of flavor is nevertheless **not yet complete**.
- * The continuing study of low-energy flavor-changing processes with increased precision will play a **crucial** role in the search for **new physics**.

Anomalous couplings of quarks

- * In many types of new physics, the new particles are heavier than their SM counterparts.
 - Their effects can be described by an **effective low-energy theory**.
- * It is possible that the effect of new physics is **mainly to modify the SM couplings between gauge bosons and certain fermions**.
- * **Anomalous top-quark couplings** have been much studied in the literature.
 - They are most tightly constrained by the $b \rightarrow s\gamma$ decay.
 - This mode does not place severe constraints on the corresponding charm-quark couplings due to the relative smallness of the charm mass.
- * It is thus **interesting** to explore **anomalous charm-quark couplings** subject to existing and future data.

Effective interactions

- * We focus on new physics affecting primarily the **charged weak currents** involving the **charm** quark.
- * The effective Lagrangian for a general parametrization of the W boson interacting with an up-type quark U_k and a down-type quark D_l can be written as

$$\mathcal{L}_{UDW} = -\frac{g}{\sqrt{2}} V_{kl} \bar{U}_k \gamma^\mu [(1 + \kappa_{kl}^L) P_L + \kappa_{kl}^R P_R] D_l W_\mu^+ + \text{H.c.}$$

g is the weak coupling constant, the anomalous couplings $\kappa_{kl}^{L,R}$ are normalized relative to the CKM-matrix elements V_{kl} , and $P_{L,R} = \frac{1}{2}(1 \mp \gamma_5)$.

- * In general, $\kappa_{kl}^{L,R}$ are complex and therefore provide **new sources of CP violation**.

Loop-induced processes

- * The anomalous quark- W couplings generate flavor-changing neutral-current interactions via
 - γ - and Z -penguin diagrams



- box diagrams



- * They therefore affect loop-induced processes, such as $K \rightarrow \pi \nu \bar{\nu}$, $K_L \rightarrow \ell^+ \ell^-$, and neutral-meson mixing.

Loop contributions

- * The effective theory with anomalous couplings is **not renormalizable**
 - This results in **divergent** contributions to some of the processes we consider.
- * These **divergences** are understood in the context of effective field theories as contributions to the coefficients of **higher-dimension operators**.
- * Numerically, we will limit ourselves to the anomalous couplings, ignoring the higher-dimension operators.
- * In so doing, we trade the possibility of obtaining precise predictions in specific models for **order-of-magnitude estimates** of the effects of **new physics** parameterized in a **model-independent** way.

Loop evaluations

- * Not having the knowledge about the new degrees of freedom, we adopt the **unitary gauge**, implying the loops contain only fermions and W -bosons.
- * We follow the common procedure of using **dimensional regularization**, dropping the resulting pole in 4 dimensions, and identifying the renormalization scale μ with the **scale of the new physics** underlying the effective theory.
- * Our results thus contain a logarithmic term of the form $\ln(\mu/m_W)$.
 - We set $\mu = \Lambda = 1 \text{ TeV}$ for definiteness.
- * We also keep in our estimates those finite terms corresponding to contributions from SM quarks in the loops.
- * In the SM limit ($\kappa^{\text{L,R}} = 0$), after CKM unitarity is imposed, our results are **finite** and **reproduce those obtained in the literature** using R_ξ gauges.

Effective Hamiltonians for $d\bar{d}' \rightarrow \nu\bar{\nu}, \ell\bar{\ell}$ induced by κ 's

- * The effective Hamiltonians generated at one loop by the anomalous charm couplings, at the m_W scale,

$$\begin{aligned} \mathcal{H}_{d\bar{d}' \rightarrow \nu\bar{\nu}}^\kappa &= \frac{\alpha G_F \lambda_c (\kappa_{cd}^L + \kappa_{cd'}^{L*})}{\sqrt{8} \pi \sin^2 \theta_W} \left(-3 \ln \frac{\Lambda}{m_W} + 4X_0(x_c) \right) \bar{d}' \gamma^\sigma P_L d \bar{\nu} \gamma_\sigma P_L \nu \\ &+ \frac{\alpha G_F \lambda_c \kappa_{cd}^R \kappa_{cd'}^{R*}}{\sqrt{8} \pi \sin^2 \theta_W} \left[(4x_c - 3) \ln \frac{\Lambda}{m_W} + \tilde{X}(x_c) \right] \bar{d}' \gamma^\sigma P_R d \bar{\nu} \gamma_\sigma P_L \nu, \end{aligned}$$

$$\begin{aligned} \mathcal{H}_{d\bar{d}' \rightarrow \ell + \bar{\ell}}^\kappa &= \frac{\alpha G_F \lambda_c (\kappa_{cd}^L + \kappa_{cd'}^{L*})}{\sqrt{8} \pi} \left[\left(3 \ln \frac{\Lambda}{m_W} - 4Y_0(x_c) \right) \frac{\bar{d}' \gamma^\sigma P_L d \bar{\ell} \gamma_\sigma P_L \ell}{\sin^2 \theta_W} \right. \\ &\quad \left. + \left(-\frac{16}{3} \ln \frac{\Lambda}{m_W} + 8Z_0(x_c) \right) \bar{d}' \gamma^\sigma P_L d \bar{\ell} \gamma_\sigma \ell \right] \\ &+ \frac{\alpha G_F \lambda_c \kappa_{cd}^R \kappa_{cd'}^{R*}}{\sqrt{8} \pi} \left\{ \left[(3 - 4x_c) \ln \frac{\Lambda}{m_W} + \tilde{Y}(x_c) \right] \frac{\bar{d}' \gamma^\sigma P_R d \bar{\ell} \gamma_\sigma P_L \ell}{\sin^2 \theta_W} \right. \\ &\quad \left. + \left[\left(8x_c - \frac{16}{3} \right) \ln \frac{\Lambda}{m_W} + \tilde{Z}(x_c) \right] \bar{d}' \gamma^\sigma P_R d \bar{\ell} \gamma_\sigma \ell \right\} \end{aligned}$$

Effective Hamiltonians induced by κ 's

* From the box diagrams

$$\begin{aligned}
 \mathcal{H}_{d\bar{d}' \rightarrow \bar{d}d'}^\kappa = & \\
 & \frac{G_F^2 m_W^2}{8\pi^2} \lambda_c (\kappa_{cd}^L + \kappa_{cd'}^{L*}) \left(-\lambda_t x_t \ln \frac{\mu^2}{m_W^2} - \sum_q \lambda_q \mathcal{B}_1(x_q, x_c) \right) \bar{d}' \gamma^\alpha P_L d \bar{d} \gamma_\alpha P_L d \\
 & - \frac{G_F^2 m_W^2}{4\pi^2} \lambda_c \kappa_{cd}^R \kappa_{cd'}^{R*} \left(\lambda_t x_t \ln \frac{\mu^2}{m_W^2} + \sum_q \lambda_q \mathcal{B}_2(x_q, x_c) \right) \bar{d}' \gamma^\alpha P_L d \bar{d} \gamma_\alpha P_R d \\
 & - \frac{G_F^2 m_W^2}{4\pi^2} \lambda_c^2 x_c \left(\ln \frac{\mu^2}{m_W^2} + \mathcal{B}_3(x_c, x_c) \right) \left[(\kappa_{cd}^{R*})^2 \bar{d}' P_R d \bar{d} P_R d + (\kappa_{cd'}^R)^2 \bar{d}' P_L d \bar{d} P_L d \right]
 \end{aligned}$$

$d' \neq d$, terms linear in κ^L and quadratic in κ^R are kept, $\lambda_q = V_{qd'}^* V_{qd}$, θ_W is the Weinberg angle, $X_0, Y_0, Z_0, \tilde{X}, \tilde{Y}, \tilde{Z}$, and $\mathcal{B}_{1,2,3}$ are loop functions.

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}$$

- * The dominant contribution in the SM comes from the top loop

$$\mathcal{M}_{\text{SM}}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = \frac{G_F}{\sqrt{2}} \frac{\alpha V_{td} V_{ts}^* X(x_t)}{2\pi \sin^2 \theta_W} \langle \pi^+ | \bar{s} \gamma_\mu d | K^+ \rangle \bar{\nu} \gamma^\mu (1 - \gamma_5) \nu$$

- * The combined SM and anomalous-charm contribution

$$\mathcal{M}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (1 + \delta) \mathcal{M}_{\text{SM}}(K^+ \rightarrow \pi^+ \nu \bar{\nu}),$$

$$\delta = \frac{V_{cd} V_{cs}^*}{V_{td} V_{ts}^*} \frac{(\kappa_{cd}^L + \kappa_{cs}^{L*}) [-3 \ln(\Lambda/m_W) + 4X_0(x_c)]}{4X(x_t)} + \mathcal{O}(\kappa^2)$$

- * The SM branching ratio

$$\mathcal{B}_{\text{SM}}(K^+ \rightarrow \pi^+ \nu \bar{\nu}) = (8.5 \pm 0.7) \times 10^{-11}$$

Buras et al.
Mescia & Smith
Brod & Gorbahn

- * Its experimental value $\mathcal{B}_{\text{exp}} = (1.73_{-1.05}^{+1.15}) \times 10^{-10}$

Artamonov et al.

- * We then require $-0.2 \leq \text{Re } \delta \leq 1$, which translates into

$$-2.5 \times 10^{-4} \leq -\text{Re}(\kappa_{cd}^L + \kappa_{cs}^L) + 0.42 \text{Im}(\kappa_{cd}^L - \kappa_{cs}^L) \leq 1.3 \times 10^{-3}$$

$$K_L \rightarrow \mu^+ \mu^-$$

- * The dominant short-distance SM contribution is also due to the top loop

$$\mathcal{M}_{\text{SM}}^{\text{SD}}(K^0 \rightarrow \mu^+ \mu^-) = -\frac{G_F}{\sqrt{2}} \frac{\alpha V_{td} V_{ts}^* Y(x_t)}{2\pi \sin^2 \theta_W} \langle 0 | \bar{s} \gamma^\sigma \gamma_5 d | K^0 \rangle \bar{\mu} \gamma_\sigma \gamma_5 \mu$$

- * The total SD amplitude

$$\mathcal{M}_{\text{SD}}(K_L \rightarrow \mu^+ \mu^-) = (1 + \delta') \mathcal{M}_{\text{SM}}^{\text{SD}}(K_L \rightarrow \mu^+ \mu^-),$$

$$\delta' = \frac{\text{Re}[V_{cd}^* V_{cs} (\kappa_{cs}^L + \kappa_{cd}^{L*})] [-3 \ln(\Lambda/m_W) + 4Y_0(x_c)]}{4 \text{Re}(V_{td}^* V_{ts}) Y(x_t)} + \mathcal{O}(\kappa^2)$$

- * The measured $\mathcal{B}(K_L \rightarrow \mu^+ \mu^-) = (6.84 \pm 0.11) \times 10^{-9}$ PDG
is almost saturated by the absorptive part of the long-distance contribution,
 $\mathcal{B}_{\text{abs}} = (6.64 \pm 0.07) \times 10^{-9}$. Littenberg & Valencia
- * The allowed room for new physics, $\mathcal{B}_{\text{NP}} \lesssim 3.8 \times 10^{-10}$, has an upper bound
 $\sim \frac{1}{2}$ the SD SM contribution, $\mathcal{B}_{\text{SM}}^{\text{SD}} = (7.9 \pm 1.2) \times 10^{-10}$. Gorbahn & Haisch
- * Consequently, we demand $|\delta'| \leq 0.2$, implying

$$\left| \text{Re}(\kappa_{cs}^L + \kappa_{cd}^L) + 6 \times 10^{-4} \text{Im}(\kappa_{cs}^L - \kappa_{cd}^L) \right| \leq 1.5 \times 10^{-4}$$

$K-\bar{K}$ mixing

- * The matrix element for $K^0-\bar{K}^0$ mixing $M_{12}^K = \langle K^0 | \mathcal{H}_{d\bar{s} \rightarrow \bar{d}s} | \bar{K}^0 \rangle / (2m_K)$ consists of SM and new-physics terms.
- * The anomalous charm contribution

$$M_{12}^{K,\kappa} = \frac{G_F^2 m_W^2}{24\pi^2} f_K^2 m_K \lambda_c^{ds} \left[\bar{\eta}^3 B_K (\kappa_{cd}^{L*} + \kappa_{cs}^L) \left(-\lambda_t^{ds} x_t \ln \frac{\mu^2}{m_W^2} - \sum_q \lambda_q^{ds} \mathcal{B}_1(x_q, x_c) \right) \right. \\ \left. + \frac{\bar{\eta}^{3/2} B_K m_K^2}{(m_d + m_s)^2} \kappa_{cd}^{R*} \kappa_{cs}^R \left(\lambda_t^{ds} x_t \ln \frac{\mu^2}{m_W^2} + \sum_q \lambda_q^{ds} \mathcal{B}_2(x_q, x_c) \right) \right]$$

$$\lambda_q^{ds} = V_{qd}^* V_{qs}$$

- * The K_L-K_S mass difference $\Delta M_K = 2 \text{Re} M_{12}^K + \Delta M_K^{\text{LD}}$ contains a sizable long-distance term, ΔM_K^{LD} .
- * Since the LD part has significant uncertainties, we constrain the κ 's by requiring that their contribution to ΔM_K be less than the largest SM contribution, arising from the charm loop,

$$M_{12}^{K,\text{SM}} \simeq \frac{G_F^2 m_W^2}{12\pi^2} f_K^2 m_K B_K \eta_{cc} (\lambda_c^{ds})^2 S_0(x_c)$$

$K-\bar{K}$ mixing

- * As a result

$$|0.043 \operatorname{Re}(\kappa_{cd}^L + \kappa_{cs}^L) + 0.015 \operatorname{Im}(\kappa_{cd}^L - \kappa_{cs}^L) - \operatorname{Re}(\kappa_{cd}^{R*} \kappa_{cs}^R) + 0.28 \operatorname{Im}(\kappa_{cd}^{R*} \kappa_{cs}^R)| \leq 8.5 \times 10^{-4}$$

- * A complementary constraint on the couplings can be obtained from the CP -violation parameter ϵ .
- * Its magnitude is related to M_{12}^K by

$$|\epsilon| \simeq \frac{|\operatorname{Im} M_{12}^K|}{\sqrt{2} \Delta M_K^{\text{exp}}}, \quad \Delta M_K^{\text{exp}} = (3.483 \pm 0.006) \times 10^{-15} \text{ GeV}$$

- * Measurements yield $|\epsilon|_{\text{exp}} = (2.229 \pm 0.012) \times 10^{-3}$ PDG
- * The SM predicts $|\epsilon|_{\text{SM}} = (2.06_{-0.53}^{+0.47}) \times 10^{-3}$ CKMfitter
- * We thus demand $|\epsilon|_{\kappa} < 0.7 \times 10^{-3}$, leading to

$$|0.015 \operatorname{Re}(\kappa_{cs}^L + \kappa_{cd}^L) + 0.043 \operatorname{Im}(\kappa_{cs}^L - \kappa_{cd}^L) - 0.28 \operatorname{Re}(\kappa_{cd}^{R*} \kappa_{cs}^R) - \operatorname{Im}(\kappa_{cd}^{R*} \kappa_{cs}^R)| \leq 2.5 \times 10^{-6}$$

Constraints from dipole penguin operators

- * Electromagnetic and chromomagnetic dipole operators describing $d \rightarrow d' \gamma$ and $d \rightarrow d' g$ are generated at one loop with W and up-type quark in the loop.
 - New-physics effects are known to give rise to potentially large corrections to SM contribution.
- * Constraints on the κ 's can be obtained from
 - $b \rightarrow s \gamma$
 - $s \rightarrow d \gamma$
 - $s \rightarrow dg$ contribution to CP -violation parameters ϵ and ϵ' in the kaon sector and $A_{\Lambda \Xi}$ in hyperon nonleptonic decays
- * The corresponding flavor-conserving contributions to the electric dipole moment of the neutron also provide constraints on some of the κ 's.

$B_{d,s}$ processes

- * B_d - \bar{B}_d mixing
- * CP -violation parameter β in $B_d \rightarrow J/\psi K_S$
 - κ terms in both mixing & decay amplitudes.
- * B_s - \bar{B}_s mixing
- * CP -violation parameter β_s in $B_s \rightarrow J/\psi\phi$
 - κ terms in both mixing & decay amplitudes

Tree-level processes

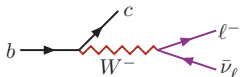
- * Anomalous charm- W couplings affect some transitions at tree level.

- * CP -conserving processes

- $(d, s)\bar{c} \rightarrow \ell^- \bar{\nu}_\ell$

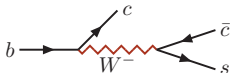


- $b \rightarrow ce^- \bar{\nu}_e$



- * CP -violating processes

- $b \rightarrow c\bar{c}s$



- * Decay constants f_D and f_{D_s} in $D \rightarrow \ell\nu$ & $D_s \rightarrow \ell\nu$.
- * Exclusive & inclusive $b \rightarrow c\ell^- \bar{\nu}_\ell$ decays.
- * Difference in $\sin\beta$ values from $B_d \rightarrow J/\psi K$ and $B_s \rightarrow \eta_c K$.

Summary of constraints

Process	Constraint
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	$-1.3 \times 10^{-3} \leq \text{Re}(\kappa_{cd}^L + \kappa_{cs}^L) + 0.42 \text{Im} \kappa_{cs}^L \leq 2.5 \times 10^{-4}$
$K_L \rightarrow \mu^+ \mu^-$	$ \text{Re}(\kappa_{cs}^L + \kappa_{cd}^L) + 6 \times 10^{-4} \text{Im} \kappa_{cs}^L \leq 1.5 \times 10^{-4}$
ΔM_K	$ 0.043 \text{Re}(\kappa_{cd}^L + \kappa_{cs}^L) - 0.015 \text{Im} \kappa_{cs}^L - \text{Re}(\kappa_{cd}^{R*} \kappa_{cs}^R) + 0.28 \text{Im}(\kappa_{cd}^{R*} \kappa_{cs}^R) \leq 8.5 \times 10^{-4}$
ϵ	$ 0.015 \text{Re}(\kappa_{cs}^L + \kappa_{cd}^L) + 0.043 \text{Im} \kappa_{cs}^L - 0.28 \text{Re}(\kappa_{cd}^{R*} \kappa_{cs}^R) - \text{Im}(\kappa_{cd}^{R*} \kappa_{cs}^R) \leq 2.5 \times 10^{-6}$
ΔM_d	$-0.031 \leq \text{Re}(\kappa_{cb}^L + \kappa_{cd}^L) + 0.4 \text{Im} \kappa_{cb}^L \leq 0.003$
$\sin(2\beta)$	$-1.5 \times 10^{-3} \leq 0.4 \text{Re}(\kappa_{cb}^L + \kappa_{cd}^L) - 0.69 \text{Im} \kappa_{cb}^L - 0.31 \text{Im} \kappa_{cs}^L \leq 0.012$
ΔM_s	$-0.014 \leq \text{Re}(\kappa_{cs}^L + \kappa_{cb}^L) + 0.018 \text{Im}(\kappa_{cs}^L - \kappa_{cb}^L) \leq 0.015$
$\sin(2\beta_s)$	$-0.09 \leq 0.026 \text{Re}(\kappa_{cb}^L + \kappa_{cs}^L) + \text{Im}(\kappa_{cb}^L - \kappa_{cs}^L) \leq 7 \times 10^{-4}$
$D \rightarrow \ell \nu$	$ \text{Re}(\kappa_{cd}^L - \kappa_{cd}^R) \leq 0.04$
$D_s \rightarrow \ell \nu$	$0 \leq \text{Re}(\kappa_{cs}^L - \kappa_{cs}^R) \leq 0.1$
$b \rightarrow c \ell \bar{\nu}$	$-0.13 \leq \text{Re} \kappa_{cb}^R \leq 0$
$B \rightarrow \psi K, \eta_c K$	$-5 \times 10^{-4} \leq \text{Im}(\kappa_{cb}^R + \kappa_{cs}^R) \leq 0.04$

Constraint on each anomalous charm coupling

- * Constraints extracted by taking only one anomalous coupling at a time to be non-zero.

$-1.5 \times 10^{-4} \leq \text{Re } \kappa_{cd}^L \leq 1.5 \times 10^{-4}$	$-6 \times 10^{-5} \leq \text{Im } \kappa_{cd}^L \leq 6 \times 10^{-5}$
$-1.5 \times 10^{-4} \leq \text{Re } \kappa_{cs}^L \leq 1.5 \times 10^{-4}$	$-6 \times 10^{-5} \leq \text{Im } \kappa_{cs}^L \leq 6 \times 10^{-5}$
$-4 \times 10^{-3} \leq \text{Re } \kappa_{cb}^L \leq 3 \times 10^{-3}$	$-0.02 \leq \text{Im } \kappa_{cb}^L \leq 7 \times 10^{-4}$
$-0.04 \leq \text{Re } \kappa_{cd}^R \leq 0.04$	$-2 \times 10^{-3} \leq \text{Im } \kappa_{cd}^R \leq 2 \times 10^{-3}$
$-0.1 \leq \text{Re } \kappa_{cs}^R \leq 0$	$-5 \times 10^{-4} \leq \text{Im } \kappa_{cs}^R \leq 2 \times 10^{-3}$
$-0.13 \leq \text{Re } \kappa_{cb}^R \leq 0$	$-5 \times 10^{-4} \leq \text{Im } \kappa_{cb}^R \leq 0.04$

- * The **left-handed** couplings are **much more constrained** than the **right-handed** one.
- * The **imaginary part** of the couplings is **more tightly constrained** than the corresponding **real part**.
- * The **largest deviations allowed** by current data appear in the **real part of the right-handed** couplings, which can be as large as **10%** of the corresponding SM couplings.

Conclusions

- * We have explored the phenomenological consequences of **anomalous W -boson couplings to the charm quark** in a **comprehensive way**.
- * The resulting constraints on the anomalous charm couplings are, perhaps surprisingly, **comparable** or **tighter** than existing constraints on anomalous W -boson couplings to the top quark.
- * Our study also **indicates out which future measurements can provide the most sensitive tests** for **new physics that can be parameterized with anomalous charm- W couplings**.