An aerial photograph of the ISTRAN complex, showing various buildings, parking lots, and green spaces. The text is overlaid on the image.

Study of $K \rightarrow \mu \nu \gamma$ decay

at

ISTRAN+ SETUP

Viacheslav Duk, INR Moscow

For ISTRAN+ collaboration

Outline

- $K \rightarrow \mu \nu \gamma$ decay
- ISTRA+ experiment
- Event selection
- Spectrum tuning
- Background rejection
- Signal extraction
- Spectrum fitting
- Results
- Conclusions

$K \rightarrow \mu \nu \gamma$ decay: introduction

- Motivation
- Differential decay rate
- F_V and F_A theoretical predictions
- Experiments

$K \rightarrow \mu \nu \gamma$ decay: motivation

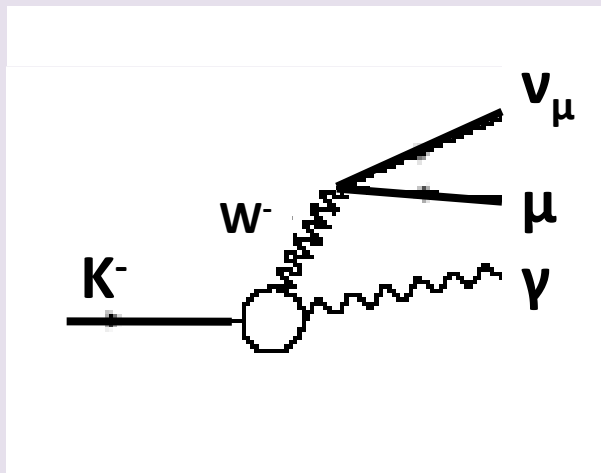
photon emitted from the vertex (SD or DE)



Probing electroweak structure of kaon



Testing predictions of ChPT, LFQM, ...



$K \rightarrow \mu \nu \gamma$ theory: differential decay rate

$$\frac{d\Gamma_{K\mu\nu\gamma}}{dx dy} = A_{IB} f_{IB}(x, y) + A_{SD} [(F_V + F_A)^2 f_{SD+}(x, y) + (F_V - F_A)^2 f_{SD-}(x, y)] - A_{INT} [(F_V + F_A) f_{INT+}(x, y) + (F_V - F_A) f_{INT-}(x, y)],$$

3 main terms:
 IB – dominant
 SD \pm , INT \pm - most interesting ($\rightarrow F_V, F_A$)

Kinematical variables:

$$x = 2 * E_\nu(\text{cm}) / M_K$$

$$y = 2 * E_\mu(\text{cm}) / M_K$$

$$f_{IB}(x, y) = \left[\frac{1 - y + r}{x^2(x + y - 1 - r)} \right] \times \left[x^2 + 2(1 - x)(1 - r) - \frac{2xr(1 - r)}{x + y - 1 - r} \right],$$

$$f_{SD+} = [x + y - 1 - r][(x + y - 1)(1 - x) - r],$$

$$f_{SD-} = [1 - y + r][(1 - x)(1 - y) + r],$$

$$f_{INT+} = \left[\frac{1 - y + r}{x(x + y - 1 - r)} \right] [(1 - x)(1 - x - y) + r],$$

$$f_{INT-} = \left[\frac{1 - y + r}{x(x + y - 1 - r)} \right] [x^2 - (1 - x)(1 - x - y) - r],$$

$$r = \left[\frac{M_\mu}{M_K} \right]^2,$$

$$A_{IB} = \Gamma_{K\mu^2} \frac{\alpha}{2\pi} \frac{1}{(1 - r)^2},$$

$$A_{SD} = \Gamma_{K\mu^2} \frac{\alpha}{8\pi} \frac{1}{r(1 - r)^2} \left[\frac{M_K}{F_K} \right]^2,$$

$$A_{INT} = \Gamma_{K\mu^2} \frac{\alpha}{2\pi} \frac{1}{(1 - r)^2} \frac{M_K}{F_K}.$$

$K \rightarrow \mu \nu \gamma$ theory: formfactors

ChPT $O(p^4)$

- $F_V + F_A = 0.137$
- $F_V - F_A = 0.055$

ChPT $O(p^6)$

- $F_V + F_A = 0.116$
- $F_V - F_A = 0.048$

LFQM

- $F_V + F_A = 0.142$
- $F_V - F_A = 0.070$

$K \rightarrow \mu \nu \gamma$: main experimental results

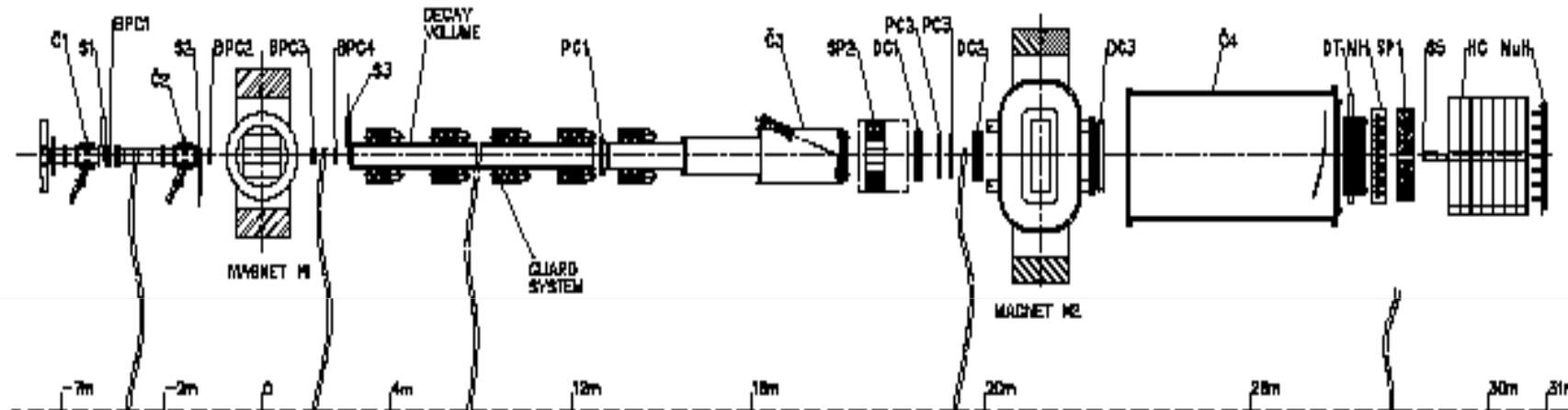
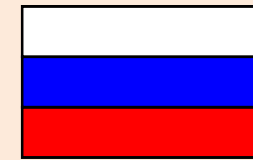
experiment	collaboration	year	cuts	results
Barmin et al		1988	$P_\mu < 231.5 \text{ MeV}/c$	BR(IB)
Demidov et al		1990	$P_\mu < 231.5 \text{ MeV}/c$	BR(IB)
Akiba et al	E104 (KEK)	1985	$214.5 < P_\mu < 231.5 \text{ MeV}/c$	BR(IB)
Adler et al	E787 (BNL)	2000	$P_\mu > 218.4 \text{ MeV}/c$ $E_\gamma > 90 \text{ MeV}$	$ F_V + F_A $, BR(SD+)

Formfactors:

E787(BNL) Phys.Rev.Lett.85(2000)2256 (K $\rightarrow\mu\nu\gamma$)
 $|F_V + F_A| = 0.165 \pm 0.013$; $-0.04 < F_V - F_A < 0.24$

E865(BNL) Phys.Rev.Lett.89(2002)061803 (K $\rightarrow e\nu e^+e^-$, K $\rightarrow\mu\nu e^+e^-$)
 $F_V + F_A = 0.147 \pm 0.026$; $F_V - F_A = 0.077 \pm 0.028$

ISTRA+ setup



$p \sim -25 \text{ GeV}$; $\Delta p/p \sim 1.5\%$; $K^- \sim 3\%$; $I \sim 3 \cdot 10^6 / 1.9 \text{ sec}$

$$T_0 = S1 \cdot S2 \cdot S3 \cdot S4 \cdot C0 \cdot C1 \cdot C2 \cdot \overline{S5}$$

(prescaled by a factor of ~ 10)

$$T_1 = T_0 \cdot (\Sigma SP1 > MIP)$$

C1-C4 – thresh. cherenkov counters; S1-S5 – scintillation counters; PC1-PC3 – proportional chambers; SP2 – veto calorimeter; SP1 – lead-glass calorimeter; DC – drift chambers; DT-drift tubes; MH – matrix scintillation godoscope

ISTRA+: from $\pi \rightarrow e \nu \gamma$ to $K \rightarrow \mu \nu \gamma$

1990

Study of $\pi \rightarrow e \nu \gamma$ decay: measuring $F_V, \gamma = F_V/F_A, F_T$

2003-
2007

- High statistics study of the decays $K^- \rightarrow e^- (\mu^-) \nu \pi^0$
 K_{e3} : Phys. Lett. B589(2004)111 ; $K_{\mu 3}$: Phys. Lett. B581(2004)31
- Measurement of the Dalitz plot slopes for $K^- \rightarrow \pi^- \pi^0 \pi^0$
Phys. Lett. B567(2003)159 .
- Search for light pseudoscalar sgoldstino in $K^- \rightarrow \pi^- \pi^0 P$
Phys.Lett.B602(2004)149-156.
- Precise measurement of Br for $K^- \rightarrow e \nu \pi^0$ Preliminary results
- Observation of the decay $K^- \rightarrow \mu^- \nu \pi^0 \gamma$
- High statistics study of the decay $K^- \rightarrow e^- \nu \pi^0 \gamma$

2009

Study of $K \rightarrow \mu \nu \gamma$ decay: measuring $F_V - F_A$

> 2009

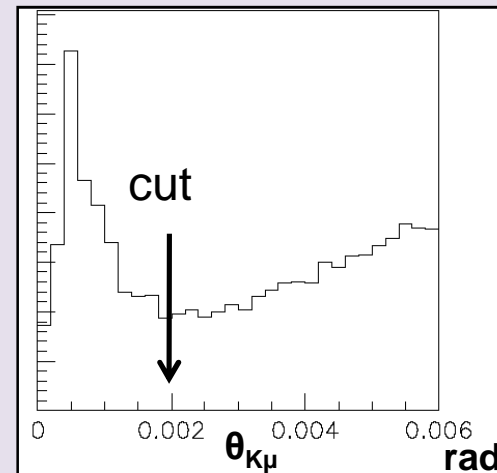
ISTRA+  **OKA** (see talk by Victor Kurshetsov)

Event selection: strategy

- Track requirements
- Photon requirements
- Vertex requirements
- Particle ID

Event selection: track requirements

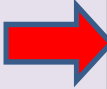
- Exactly one beam track in each projection
- Exactly one secondary track in each projection
- Secondary track is negatively charged
- track quality $> 10^{-2}$ for each projection of beam track
- track quality > 0.1 for each projection of secondary track
- Angle between beam and secondary track $> 2\text{mrad}$
(suppression of undecayed particles)

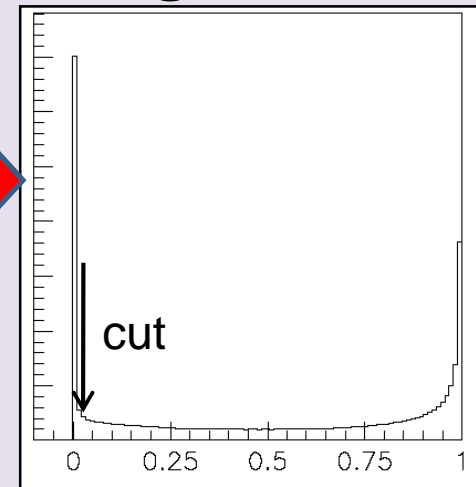


Event selection: photon requirements

- No photons in SP2 guard calorimeter
- No photons in GS

Event selection: vertex requirements

- $-3 < x < 3$ cm
- $-2 < y < 6$ cm
- $400 < z < 1600$ cm
(decay volume: 300-1200cm, SP2 guard calorimeter: $z=1650$ cm)
- Vertex fit probability > 0.01 



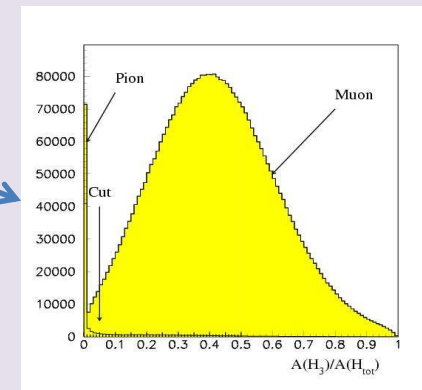
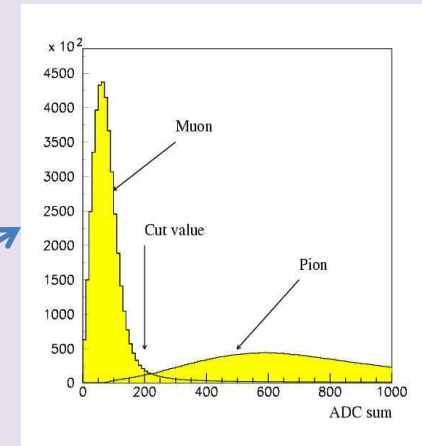
Event selection: particle ID

- **Photon**: shower in ECAL
not associated with any track

- **Muon**:

- 1) ADC sum in HCAL < 200

- 2) relative energy deposition in
last 3 layers of HCAL > 0.05



Spectrum tuning: strategy

- Trigger efficiency for photon
- Muon momentum kinematical calibration
- Photon energy kinematical calibration

Trigger efficiency ε for photon

Data structure:

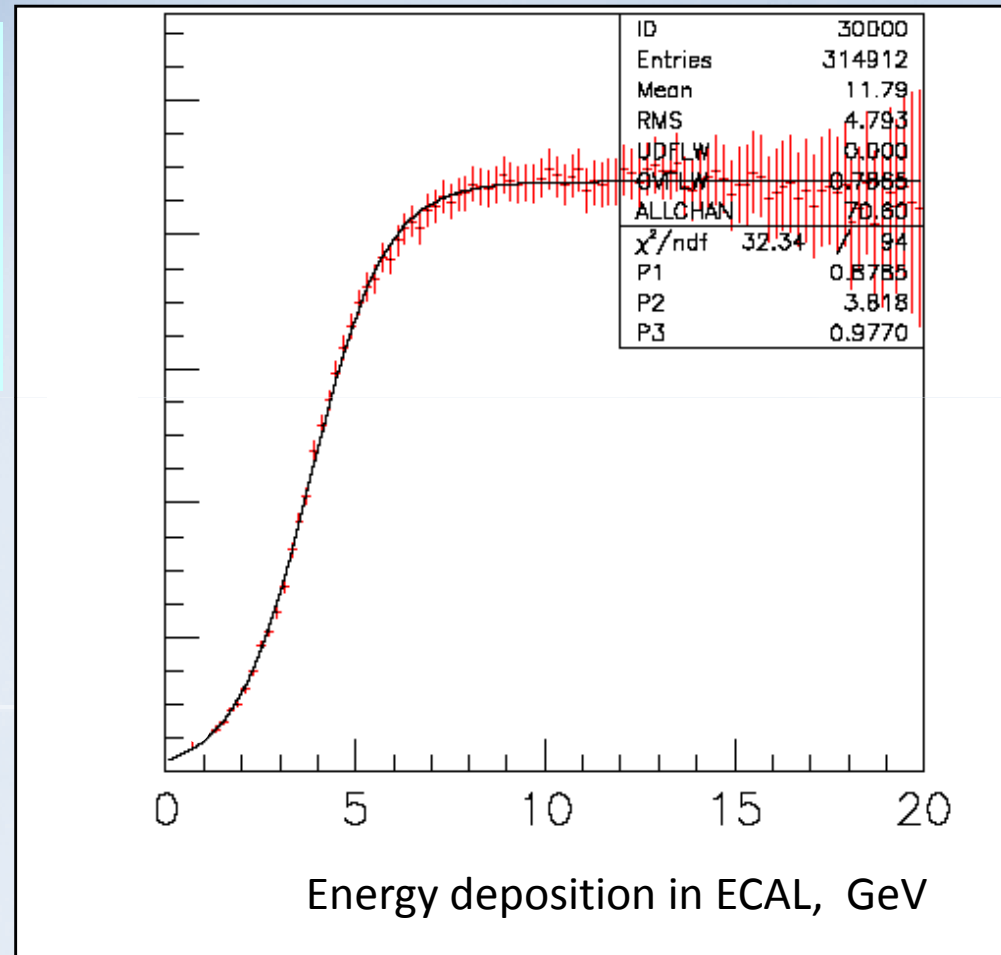
T_0 trigger: ~10%

$T_1 = T_0 \cdot (\sum ECAL > MIP) : \sim 90\%$

Trigger efficiency:

$$\varepsilon = T_0 \cdot T_1 / T_0$$

**Data with T_1 are
weighted by $1/\varepsilon$**



Kinematical calibration

- General idea: use of 2-body kinematics
- P_μ tuning: peaks in $K\mu 2$ and $K\pi 2$ must correspond to table values
- E_γ tuning: a peak in $E_{\pi 0}$ for $K\pi 2$ selection must correspond to table value

Background rejection

- Main backgrounds
- Primary cuts
- Kinematical variables and signal observation

Background rejection

- Main background:



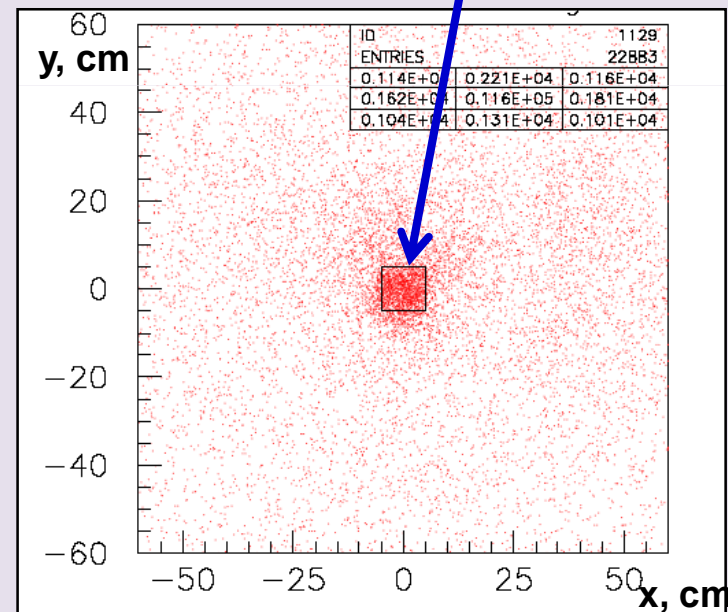
with 1 gamma lost (from $\pi^0 \rightarrow \gamma\gamma$)



with 1 gamma lost (from $\pi^0 \rightarrow \gamma\gamma$) and π misidentification

Background rejection: primary cuts

- Missing momentum in ECAL plane: central hole region is dominated by $K\pi 2$ and excluded
- Y-distance between muon and photon in ECAL plane:
 $-20 < dy < 50$ cm



Background rejection: kinematical variables

- Signal observation:

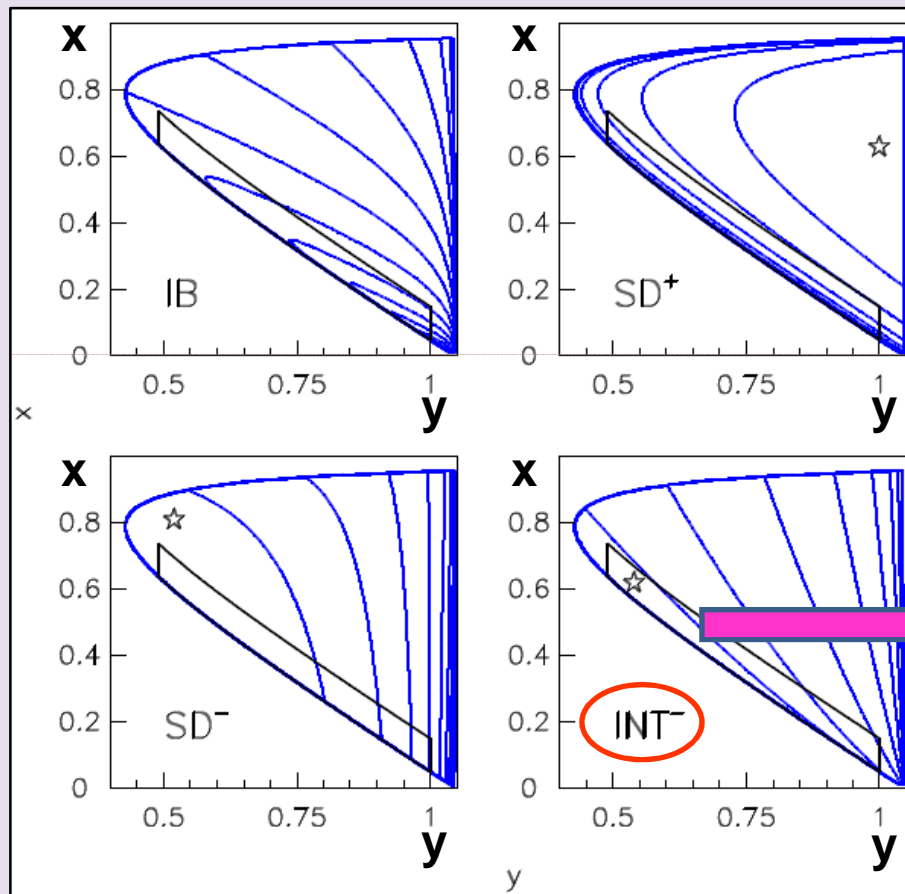
$$M(\mu \nu \gamma) = \sqrt{(P_\mu + P_\nu + P_\gamma)^2} \text{ where}$$

$$\vec{p}_\nu = \vec{p}_K - \vec{p}_\mu - \vec{p}_\gamma ; \quad E_\nu = |\vec{p}_\nu|$$

$M(\mu\nu\gamma)$ peaks at $M_K = 0.494$ GeV for signal

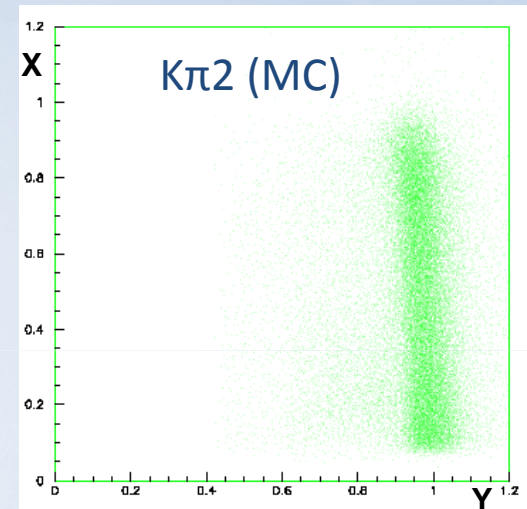
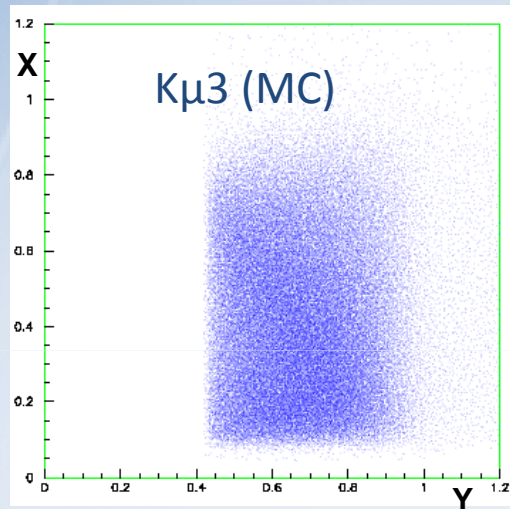
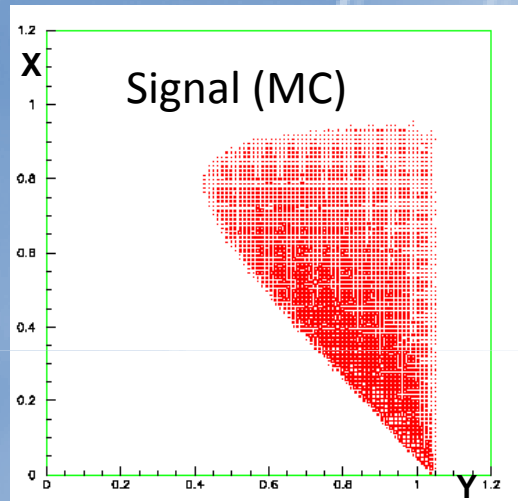
Background rejection procedure: scanning over (x,y) Dalits-plot and looking for a peak in $M(\mu\nu\gamma)$

Background rejection: Dalits-plot plot signal



***Our strategy:
Focusing on INT⁻ region***

Background rejection: (x,y) Dalits plot



Previous experiments: looking for signal near y kinematical border

ISTRA+: looking for signal near E_ν kinematical border

Signal extraction: strategy

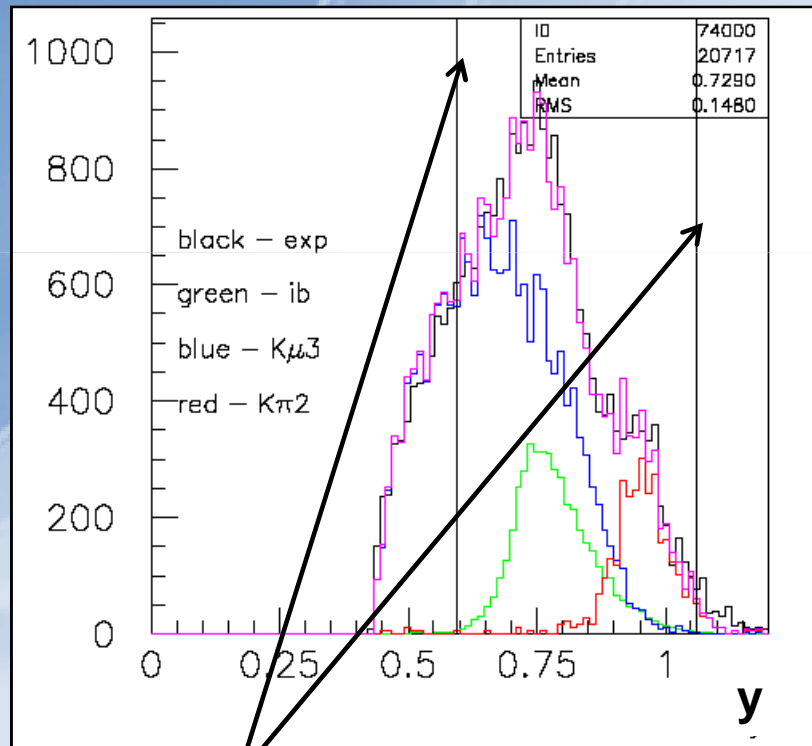
- X-stripes and distribution over y in x-stripes
- Cut on y in x-stripes
- $M(\mu \nu \gamma)$ in xy -stripes

Signal extraction: X-stripes, distribution over y , cut on y

- (x,y) dalits-plot is divided into **stripes** with $\delta x=0.05$ width (x-stripes)
- A cut on y is put in each stripe (xy-stripe)
- Ratio $R=S/\sqrt{(S+B)}$ (S – number of INT- events, B – IB+background) is used for putting cut on y within a particular stripe
- Maximum of R corresponds to minimal error

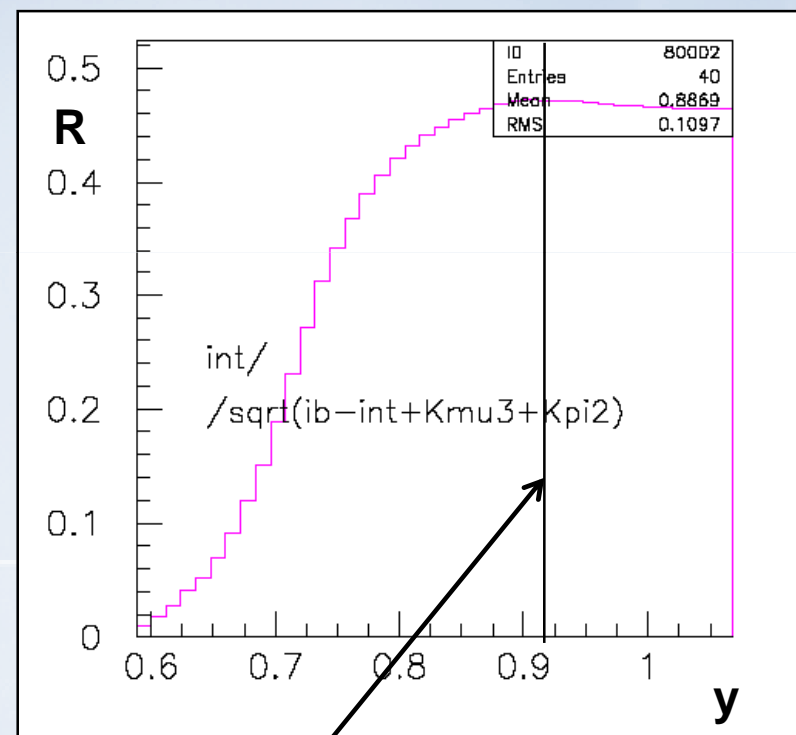
Signal extraction: X-stripes, distribution over y , cut on y

Y in x-stripe



Limits for R calculation

Ratio R in x-stripe



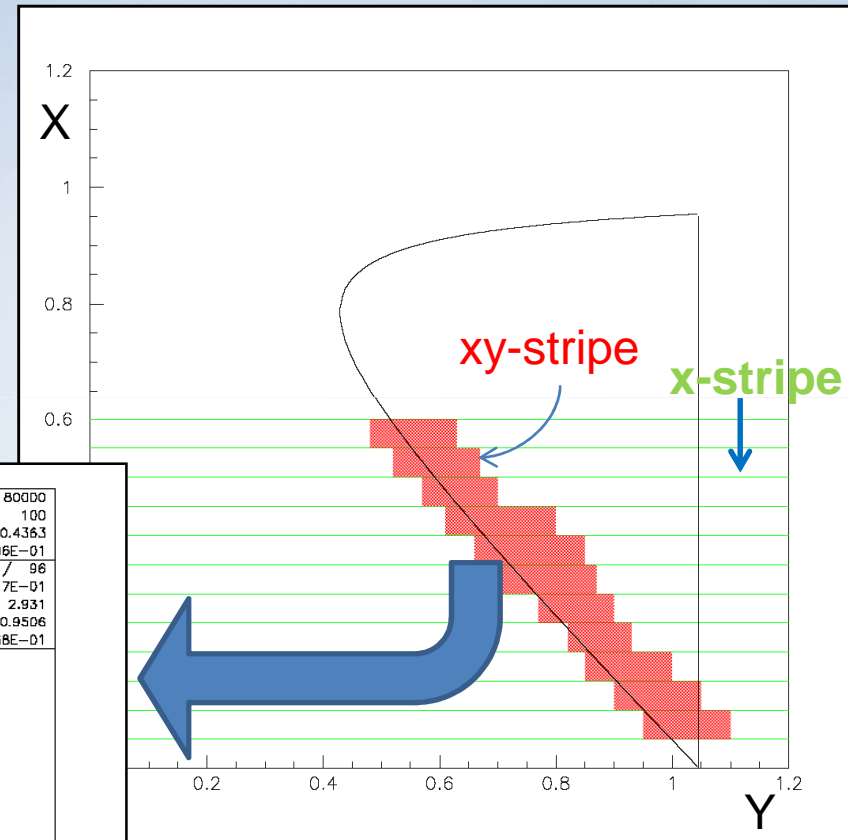
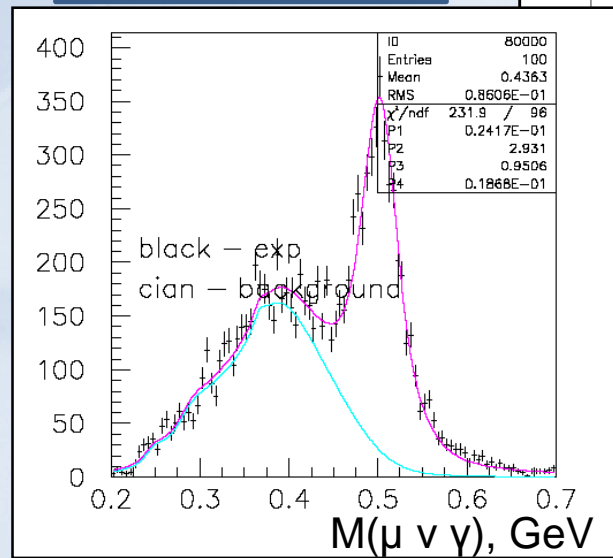
Putting upper cut on y

Signal extraction: fitting $M(\mu \nu \gamma)$ in xy -stripes

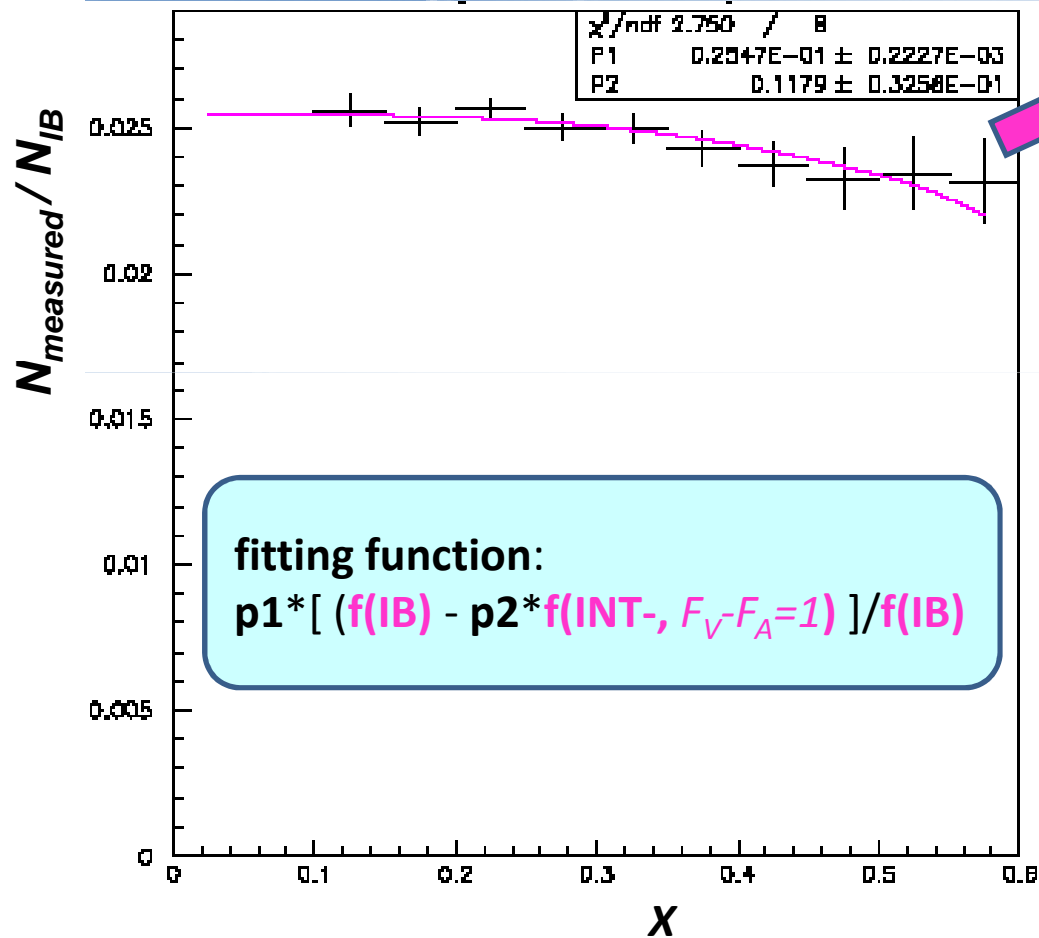
~44000 events extracted

fitting $M(\mu \nu \gamma)$ in xy -stripe

Signal and background shapes taken from MC



Spectrum fitting



- N(IB) is taken from MC
- Negative sign of INT- clearly seen
- ~2% effect of INT-

Preliminary result:

$$F_V - F_A = 0.12 \pm 0.03 \pm 0.03$$

$F_V - F_A$: comparison with theory

$$F_V - F_A = 0.12 \pm 0.03(\text{stat}) \pm 0.03(\text{syst})$$

ChPT $O(p^4)$

$$F_V - F_A = 0.055$$

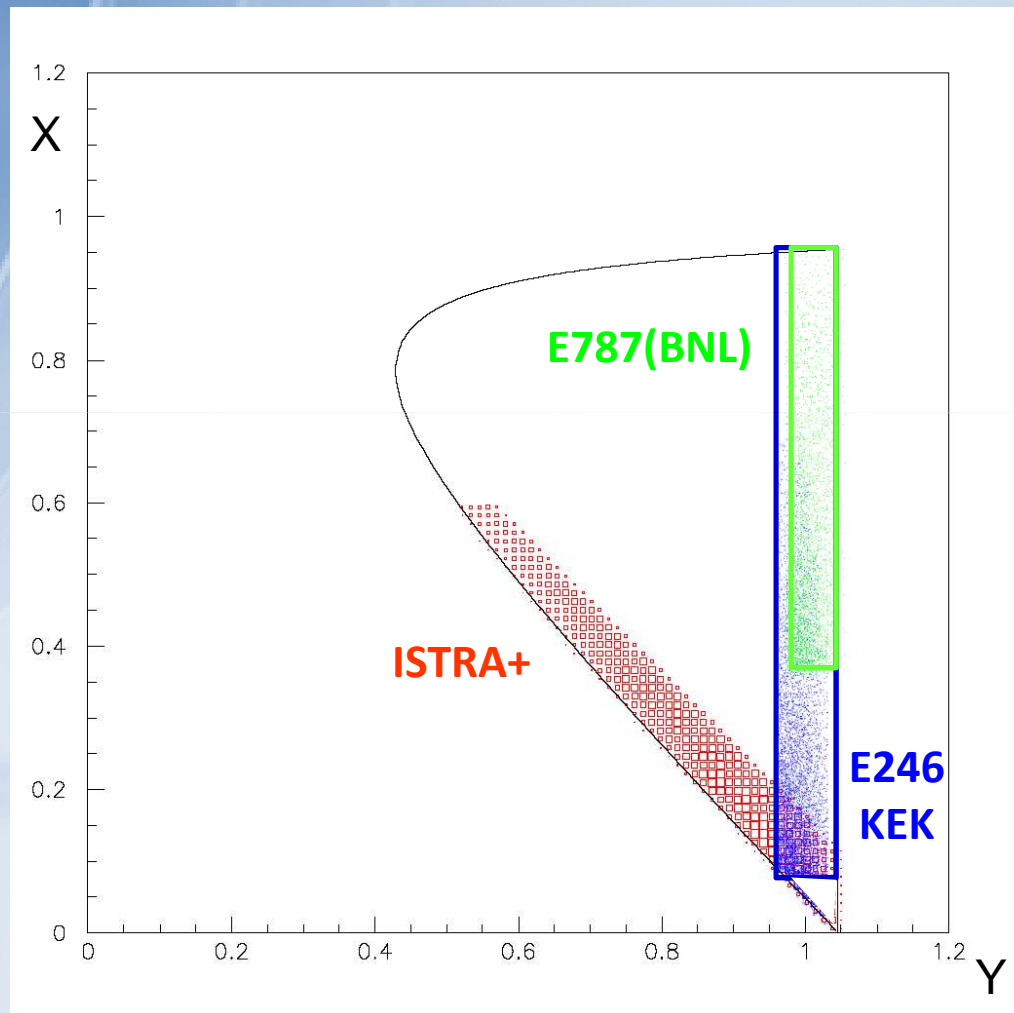
ChPT $O(p^6)$

$$F_V - F_A = 0.048$$

LFQM

$$F_V - F_A = 0.070$$

ISTRA+ kinematical region: complementary with previous experiments



ISTRA+ result: complementary with previous experiments

experiment	collaboration	year	cuts	results
Barmin et al		1988	$P_\mu < 231.5 \text{ MeV}/c$	BR(IB)
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Adler et al	E787 (BNL)	2000	$P_\mu > 218.4 \text{ MeV}/c$ $E_\gamma > 90 \text{ MeV}$	$ F_V + F_A $
Akimenko et al	ISTRA+	2009	$E_\gamma < 148 \text{ MeV}$ ($x < 0.6$)	$F_V - F_A$

E787: 2800 events
ISTRA+: 44000 events

**~15 times larger
statistics**

conclusion

- The $K \rightarrow \mu \nu \gamma$ decay is observed at ISTRA+ setup in a new kinematical region
- The **event number** observed is **44K** (the largest statistics in the world)
- First measurement of INT- term gives **$F_V - F_A = 0.12 \pm 0.03(\text{stat}) \pm 0.03(\text{syst})$**
- The sign of INT- is negative
- The results are preliminary

To KAON09 organizers and participants

THANK YOU!!!